Insertion Sort

Input: Array $A[1..n]$

Output: Array $A$ is sorted

1) for $j \leftarrow 2$ to $n$
2) $x = A[j]$
3) $i = j - 1$
4) while $(i > 0$ and $A[i] > x)$
5) $A[i+1] \leftarrow A[i]$
6) $i \leftarrow i - 1$
7) $A[i+1] \leftarrow x$

endfor

Figure 1: Insertion Sort

1 Analysis - Version 1.2

The number of times each instruction is executed is given below.

1. The for loop has 1 assignment, $n$ comparisons, and another $n-1$ assignments (the increment).
2. $n-1$ assignments, each with an extra memory access
3. $n-1$ assignments
4. $2t_j + 2$ comparisons checking the condition in the while loop for each $j$, where $t_j$ is the number of elements of the array we need to move to insert $A[j]$ among $A[1], \ldots, A[j-1]$. Another $t_j + 1$ AND operations. Total: $3(n-1) + 3 \sum_{j=2}^{n} t_j$
5. $t_j$ assignments for each $j$, with two extra memory access each. Total: $\sum_{j=2}^{n} t_j$
6. $t_j$ assignments for each $j$. Total: $\sum_{j=2}^{n} t_j$
7. $n-1$ assignments, each with an extra memory access

The total overall is $n + 3(n-1) + 2 \sum_{j=2}^{n} t_j$ assignments and $n + 2(n-1) + 2 \sum_{j=2}^{n} t_j$ comparisons, and another $(n-1) + \sum_{j=2}^{n} t_j$ AND operations. Total $2n + 6(n-1) + 5 \sum_{j=2}^{n} t_j$ “elementary” operations. Each assignment involves several (here, up to five) LOAD and STORE operations, as well as several arithmetic operations.