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## Final Exam

May 4th, 2022 8:00-10:00

# CS520 - Data Integration, Warehousing, and Provenance <br> Results 

Please leave this empty.


## Part 1.1 Provenance (Total: 30 Points)

For each of the queries shown in the following compute the provenance of all of their result tuples produced over the database shown below. Calculate provenance for these provenance models:

- Minimal Why-Provenance
- Provenance Polynomials

List all query result tuples and show the provenance on the right for each query result tuple.
Consider the following database schema and instance:

> city

| name | population | state |  |
| :---: | :---: | :---: | :---: |
| Chicago | 3200000 | IL | $c_{1}$ |
| Schaumburg | 70000 | IL | $c_{2}$ |
| Evanston | 120000 | IL | $c_{3}$ |
| Seattle | 800000 | WA | $c_{4}$ |
| Austin | 2000000 | TX | $c_{5}$ |

## connection

| from | to | connectiontype | price | miles |
| :---: | :---: | :---: | :---: | :---: |
| Chicago | Seattle | flight | 540 | 2000 |
| Chicago | Austin | flight | 430 | 1500 |
| $n_{1}$ |  |  |  |  |
| Chicago | Austin | bus | 80 | 1500 |
| $n_{2}$ |  |  |  |  |
| Chicago | Schaumburg | bus | 5 | 2000 |
| Chicago | Seattle | train | 250 | 2000 |
| $n_{4}$ |  |  |  |  |
| Schaumburg | Evanston | bus | 15 | 2000 |
| Austin | Seattle | flight | 890 | 2000 |
| $n_{6}$ |  |  |  |  |
| $n_{7}$ |  |  |  |  |

## Question 1.1.1 (9 Points)

$$
\pi_{t o}\left(\sigma_{\text {price }<100 \wedge \text { from }=\text { Chicago }}(\text { connection })\right)
$$

## Solution

Minimal Why:

| to |  |
| :---: | :---: |
| Austin |  |
| Schaumburg | $\left\{\left\{n_{3}\right\}\right\}$ |
| $\left.\left\{n_{4}\right\}\right\}$ |  |

Provenance Polynomials:

| to |  |
| :---: | :---: |
| Austin | $n_{3}$ |
| Schaumburg | $n_{4}$ |

## Question 1.1.2 (10 Points)

$$
\begin{aligned}
& q_{1} \stackrel{\text { def }}{=} \pi_{\text {name }}\left(\sigma_{\text {state }=I L}(\text { city })\right) \\
& q \stackrel{\text { def }}{=} \pi_{\text {from }, \text { to }}\left(q_{1} \bowtie_{\text {name }=\text { from }}\right. \text { connection } \\
&\left.\bowtie_{t o=\text { name }} q_{1}\right)
\end{aligned}
$$

## Solution

Minimal Why provenance:

| from | to |  |
| :---: | :---: | :---: |
| Chicago | Schaumburg | $\left\{\left\{c_{1}, n_{4}, c_{2}\right\}\right\}$ |
| Schaumburg | Evanston | $\left\{\left\{c_{2}, n_{6}, c_{3}\right\}\right\}$ |

## Provenance Polynomials:

| from | to |
| :---: | :---: |
| Chicago | Schaumburg |
| $c_{1} \cdot n_{4} \cdot c_{2}$ |  |
| Schaumburg | Evanston |
| $c_{2} \cdot n_{6} \cdot c_{3}$ |  |

## Question 1.1.3 (11 Points)

$q_{1} \stackrel{\text { def }}{=} \pi_{\text {from }, \text { to }}\left(\sigma_{\text {to=Seattle }}(\right.$ connection $\left.)\right)$
$q_{2} \stackrel{\text { def }}{=} \pi_{\text {from }, \text { to }}\left(\sigma_{\text {middle }=\text { Austin }}\left(\rho_{\text {middle } \leftarrow t o}(\right.\right.$ connection $) \bowtie \rho_{\text {middle } \leftarrow \text { from }}($ connection $\left.\left.)\right)\right)$ $q \stackrel{\text { def }}{=} q_{1} \cup q_{2}$

## Solution

Minimal Why provenance:

| from | to |  |  |
| :---: | :---: | :---: | :---: |
| Chicago | Seattle | $\left\{\left\{n_{1}\right\},\left\{n_{5}\right\},\left\{n_{2}, n_{7}\right\},\left\{n_{3}, n_{7}\right\}\right\}$ |  |
| Austin | Seattle | $\left\{n_{7}\right\}$ |  |

## Provenance Polynomials:

| from | to |  |
| :---: | :---: | :---: |
| Chicago | Seattle | $n_{1}+n_{5}+n_{2} \cdot n_{7}+n_{3} \cdot n_{7}$ |
| Austin | Seattle | $n_{7}$ |

## Part 1.2 Data Warehousing (Total: 35 Points)

Recall that you should write all queries according to the schema and not according to the example instance.
Consider the following datawarehouse schema (star schema) and partial example instance. There is a single fact table (sales) about sales of items. Each row in this fact table stores the quantity of a certain product (e.g., 3 Samson Galaxy phones) sold at a particular location and time to a particular customer. There are four dimension tables corresponding to the following dimensions:

- Time with three levels (year, month, day)
- Location with four levels (state, city, zip, street)
- Customer with one level (name).
- Product with three levels (category, brand, pname, price) where pname is the finest granularity and brand and category are not comparable (some brands can have products from multiple categories and categories obviously can contain have products from different brands). The same holds for price and brand and price and category.
sales

| TID | LID | CID | PID | numItems |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 4 | 1 | 1 | 15 |
| 2 | 1 | 5 | 2 | 10 |
| 100 | 1 | 76 | 4 | 22 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

timeDim

| TID | year | month | day |
| :---: | :---: | :---: | :---: |
| 1 | 2010 | 1 | 1 |
| 2 | 2010 | 1 | 2 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| $\ldots$ | 2018 | 5 | 1 |

customerDim

| CID | cname |
| :---: | :---: |
| 1 | Noekig |
| 2 | Prokig |
| $\ldots$ | $\ldots$ |

## locationDim

| LID | state | city | zip | street |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Illinois | Chicago | 60616 | 10 W 31st |
| 2 | Illinois | Chicago | 60615 | 900 Cottage Grove |
| 3 | Lousiana | New Orleans | 42345 | 12 Mark street |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

## productDim

| PID | category | brand | pname | price |
| :---: | :---: | :---: | :---: | :---: |
| 1 | computers | Apple | MacBook | 1300 |
| 2 | computers | Dell | Inspire | 1000 |
| 3 | smartphones | Samsung | Galaxy 1 | 600 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

## Hints:

- Attributes with black background form the primary key of a relation (e.g., PID for relation productDim)
- Attributes LID, TID, PID, and CID in the fact table are foreign keys to the dimension tables


## Question 1.2.1 (8 Points)

Write an SQL query that returns for each year a breakdown of the total revenue for each level of the location dimension. The revenue of a sale is the number of items (numItems) multiplied by product's price (price).

## Solution

```
SELECT sum(numItems * price) AS revenue,
    year,
    state,
    city,
    zip,
    street,
    GROUPING(state),
    GROUPING(city),
    GROUPING(zip),
    GROUPING(street)
    FROM sales s, locationDim l, productDim p, timeDim t
WHERE s.LID = l.LID AND s.PID = p.PID AND s.TID = t.TID
GROUP BY year, ROLLUP(state, city,zip,street);
```


## Question 1.2.2 (9 Points)

Write an SQL query that returns the top-3 states with the highest average of the yearly total number of products sold in this state.

## Solution

```
SELECT avg(totalitems) AS avgyearly, state
FROM (SELECT sum(numItems) AS totalitems, state, year
    FROM sales s, locationDim l, timeDim t
    WHERE s.LID = l.LID AND s.PID = p.PID AND s.TID = t.TID
    GROUP BY state, year)
ORDER BY avgyearly DESC
LIMIT 3;
```


## Question 1.2.3 (9 Points)

Write an SQL query that returns cities with at least 3 times the number of items sold in this city than the average number of items sold in cities in the same state.

## Solution

```
WITH cityitems AS (
    SELECT sum(numItems) as totalitems, city, state
        FROM sales s, locationDim l
        WHERE s.LID = l.LID
        GROUP BY city, state),
    avgstateitems AS (
        SELECT avg(totalitems) avgitems, state
            FROM cityitems
            GROUP BY state)
SELECT city, totalitems
    FROM cityitems c,
            avgstateitems a
    WHERE c.state = a.state
        AND totalitems >= 3 * avgitems;
```


## Question 1.2.4 (9 Points)

Write an SQL query that returns all cities. For each city report its rank in terms of the total revenue (number of items (numItems) multiplied by the product price) produced by products sold in the city in 2022 compared to all other cities in the same state in 2022. Order the results by the city's revenue in decreasing order. For the ordering the state should be ignored.

## Solution

```
SELECT city,
    rank() OVER (PARTITION BY state ORDER BY revenue DESC) AS rank,
    revenue
    FROM (SELECT sum(numItems * price) AS revenue, city, state
            FROM sales s, locationDim l, timeDim t
            WHERE s.TID = t.TID
                AND s.LID = l.LID
                AND t.year = 2022
            GROUP BY city, state) cityrevs
ORDER BY revenue DESC;
```


## Part 1.3 Virtual Data Integration (Total: 35 Points)

Consider the following global schema and LAV views defining the content of local sources.

- Artist(name,age)
- Song(title,length,writtenby)
- AlbumSong(songtitle,albumtitle,nr)
- Album(title,price,genre,recordedby)

```
v1(Name,Age,Genre) :- artist(Name,Age), album(AT,P,Genre,Name), Age < 50.
v2(AlbumTitle,Performer) :- album(AlbumTitle,P,G,Performer), G = jazz.
v3(AlbumTitle) :- album(AlbumTitle,P,G,Performer), P > 30.
v4(SongTitle,AlbumTitle,WrittenBy) :- albumsong(SongTitle,AlbumTitle,N),
    song(SongTitle,L,WrittenBy),
    artist(WrittenBy,A).
```


## Question 1.3.1 (35 Points)

Rewrite the following query using the bucket algorithm with the views given above. First write down the content of the buckets, then write down every candidate rewriting based on the buckets and demonstrate whether it is a contained rewriting or not, and then write down the maximally contained UCQ rewriting for the query.

```
q(Writer,Performer,Age,Title) :- artist(Performer,Age),
    album(T,P,G,Performer),
    albumsong(Title,T,N),
    song(Title,L,Writer).
```


## Solution

First we need to create a bucket for every goal and put in each bucket the views which have the goal's relation in their body and return the head variables of the query coming from this goal.

| artist(Performer,Age) | album(T,P,G,Performer) | albumsong(Title,T,N) | song(Title,L,Writer) |
| :---: | :---: | :---: | :---: |
| v1(Performer,Age,X1) | v1(Performer,X2,X3) | v4(Title,X6,X7) | $\mathrm{v} 4($ Title,X8,Writer) |
|  | $\mathrm{v} 2(\mathrm{X} 4$, Performer $)$ |  |  |

There are three possible combinations of views to cover the goals according to the buckets.
Option 1:
We would have to add an additional equality predicate for the repeated variable T (album title). However, the view we use to cover goal album (T,P,G,Performer), does not return the album title, so this is not possible. Thus, option 1 can not be extended into a contained rewriting, no matter which additional equality constraints we add.

```
q1(Writer,Performer,Age,Title) :- v1(Performer,Age,X1), v1(Performer,X2,X3),
    v4(Title,X6,X7), v4(Title,X8,Writer).
```


## Option 2:

Note that we have to add the equality predicate $\mathrm{X} 4=\mathrm{X} 6$ to simulate the repeated variable T . Optionally, we can equate X 7 with Writer, but that is not required for containment.

```
q2a(Writer,Performer,Age,Title) :- v1(Performer,Age,X1), v2(X4,Performer),
    v4(Title,X6,X7), v4(Title,X8,Writer), X4=X6.
```

or equivalently

```
q2(Writer,Performer,Age,Title) :- v1(Performer,Age,X1), v2(X4,Performer),
    v4(Title,X4,X7), v4(Title,X8,Writer).
```

To prove containment, we have to replace the views with their definition (renaming existentially quantified variables) and then find a containment mapping from q to the expanded view.
q2(Writer, Performer, Age,Title) :- artist(Performer, Age), album(Y1,Y2,X1,Performer), Age < 50,
album(X4,Y3, Y4,Performer), Y4 = jazz,
albumsong(Title, $\mathrm{X} 4, \mathrm{Y} 5$ ),
song(Title, Y6, X7),
artist(X7,Y7),
albumsong (Title, X8,N),
song(Title, Y8, Writer),
artist(Writer,A).
Since there exists a containment mapping $\Psi$ as shown below, $q 2$ is a contained rewriting. And because this is the only contained rewriting, it is also a maximally contained rewriting.

$$
\begin{aligned}
\Psi(\text { Writer }) & \rightarrow \text { Writer } & \Psi(\text { Performer }) & \rightarrow \text { Performer } \\
\Psi(\text { Title }) & \rightarrow \text { Title } & \Psi(T) & \rightarrow X 4 \\
\Psi(G) & \rightarrow Y 4 & \Psi(N) & \rightarrow Y 5
\end{aligned}
$$

Applying this containment mapping to the goals of $q$ we get:

$$
\begin{aligned}
\Psi(\operatorname{artist}(\text { Performer }, \text { Age })) & =\operatorname{artist}(\text { Performer }, \text { Age }) \\
\Psi(\operatorname{album}(T, P, G, \text { Performer })) & =\operatorname{album}(X 4, Y 3, Y 4, \text { Performer }) \\
\Psi(\operatorname{albumsong}(\text { Title }, T, N)) & =\operatorname{albumsong}(\text { Title }, X 4, Y 5) \\
\Psi(\operatorname{song}(\text { Title }, L, W \text { riter })) & =\operatorname{song}(\text { Title }, Y 8, \text { Writer })
\end{aligned}
$$

