

ILLINOIS INSTITUTE OF TECHNOLOGY

# CS520



## Data Integration, Warehousing, and Provenance

### 1. Introduction

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## Outline

- 0) Course Info
- 1) Introduction**
- 2) Data Preparation and Cleaning
- 3) Schema matching and mapping
- 4) Virtual Data Integration
- 5) Data Exchange
- 6) Data Warehousing
- 7) Big Data Analytics
- 8) Data Provenance




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## Overview

- Topics covered in this part
  - Heterogeneity and Autonomy
  - Data Integration Tasks
  - Data Integration Architectures (Methods)
  - Some Formal Background (sorry!)

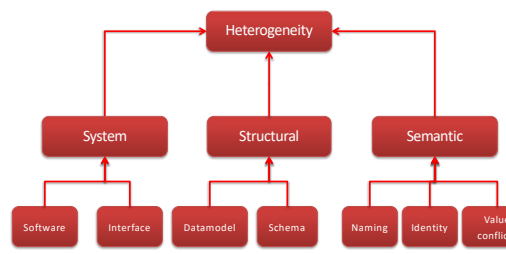


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## 1.1 Heterogeneity + Autonomy

- Taxonomy of Heterogeneity



```

graph BT
    Heterogeneity --> System
    Heterogeneity --> Structural
    Heterogeneity --> Semantic
    System --> Software
    System --> Interface
    Structural --> Datamodel
    Structural --> Schema
    Semantic --> Naming
    Semantic --> Identity
    Semantic --> ValueConflicts[Value conflicts]
    
```





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## 1.1 System Heterogeneity

- Hardware/Software
  - Different hardware capabilities of sources
  - Different protocols, binary file formats, ...
  - Different access control mechanism
- Interface Heterogeneity
  - Different interfaces for accessing data from a source
    - HTML forms
    - XML-Webservices
    - Declarative language






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## 1.1 System Heterogeneity

- Hardware/Software
  - Different hardware capabilities of sources
    - **Mobile phone vs. server:** Cannot evaluate cross-product of two 1GB relations on a mobile phone
  - Different protocols, binary file formats, ...
    - **Order information stored in text files:** line ending differs between Mac/Window/Linux, character encoding
  - Different access control mechanism
    - **FTP-access to files:** public, ssh authentication, ..

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### 1.1 System Heterogeneity

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- Interface Heterogeneity
  - Different interfaces for accessing data from a source
    - HTML forms
    - Services (SOA)
    - Declarative language
    - Files
    - Proprietary network protocol
    - ...

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### 1.1 System Heterogeneity

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- Interface Heterogeneity – Expressiveness
  - Keyword-search vs. query language
  - Predicates:** equality ( $=$ ), inequality ( $<$ ,  $!=$ )
  - Logical connectives:** conjunctive (AND), disjunctive (OR), negation
  - Complex operations:** aggregation, quantification
  - Limitations:** restriction to particular tables, predicates, fixed queries with parameters, ...

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### 1.1 System Heterogeneity

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- Interface Heterogeneity – Examples
  - Google search (+/-, site:, intitle:, filetype:)

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### 1.1 System Heterogeneity

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- Interface Heterogeneity – Examples
  - SQL

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### 1.1 System Heterogeneity

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- Interface Heterogeneity – Examples
  - SQL

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### 1.1 System Heterogeneity

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- Interface Heterogeneity – Examples
  - Web-form (with DB backend?)
    - Keyword search
    - Fixed choices
    - "Bound parameter"

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### 1.1 System Heterogeneity

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- Interface Heterogeneity – Examples
  - Email-client

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### 1.1 System Heterogeneity

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- Problems with interface heterogeneity
  - Global query language is more powerful
    - User queries may not be executable
    - Integration system has to evaluate part of the query
  - Bound parameters are incompatible with query
    - User query may not be executable

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### 1.1 System Heterogeneity

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- Example: more expressive global language
  - SQL with one table
    - books (title, author, year, isbn, genre)
  - Web form for books about history shown below
  - What problems do may arise translating user queries?

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### 1.1 System Heterogeneity

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- Integration system has to process part of the query

```

SELECT title
FROM books
WHERE author = 'Steven King'
AND year = 2012;
    
```

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### 1.1 System Heterogeneity

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- Query requires multiple requests

```

SELECT title
FROM books
WHERE author LIKE '%King%';
    
```

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### 1.1 System Heterogeneity

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- Query cannot be answered

```

SELECT title
FROM books
WHERE genre = 'SciFi';
    
```

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### 1.1 Heterogeneity + Autonomy

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- Taxonomy of Heterogeneity

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### 1.1 Structural Heterogeneity

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- Data model
  - Different semantic/expressiveness
  - Different structure
- Schema
  - Integrity constraints, keys
  - Schema elements:
    - use attribute or separate relations)
  - Structure:
    - e.g., normalized vs. denormalized relational schema

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### 1.1 Structural Heterogeneity

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- Data model
  - Relational model
  - XML model
  - Object-oriented model
  - Ontological model
  - JSON
  - ...

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### 1.1 Structural Heterogeneity

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- Example: data model
  - Relational model
  - XML model
  - JSON
  - OO
- Person and their addresses

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### 1.1 Structural Heterogeneity

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- Schema
  - Modeling choices
    - Relation vs. attribute
    - Attribute vs. value
    - Relation vs. value
  - Naming
  - Normalized vs. denormalized (relational concept)
  - Nesting vs. reference

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### 1.1 Structural Heterogeneity

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Example: Modeling choices

```

Male(id, firstname, lastname)
Female(id, firstname, lastname)
Person(id, firstname, lastname, male, female)
Person(id, firstname, lastname, gender)
    
```

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### 1.1 Structural Heterogeneity

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- **Relation-relation conflicts**
  - Naming conflicts
    - Relations with different name representing the same data (**synonym**)
    - Relations with same name representing different information (**homonym**)
  - Structural conflicts
    - Missing attributes
    - Many-to-one
    - Missing, but derivable attributes
  - Integrity constraint conflicts

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### 1.1 Structural Heterogeneity

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**Example: Conflicts between relations**

```

Person(id, firstname, lastname, male, female)
Person(id, name, gender, birthday)
Manager(id, name, gender, age)
    
```

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### 1.1 Structural Heterogeneity

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**Example: Conflicts between relations**

```

Person(id, first_name, lastname, male, female)
Person(id, name, gender, birthday)
Manager(id, name, gender, age)
    
```

Multiple attribute vs one attribute

Missing derivable attribute: Role

Derivable attribute: Compute age from birthday

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### 1.1 Structural Heterogeneity

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- **Attribute-attribute conflicts**
  - Naming conflicts
    - Attributes with different name representing the same data (**synonym**)
    - Attributes with same name representing different information (**homonym**)
  - Default value conflict
  - Integrity constraint conflicts
    - Datatype
    - Constraints restricting values

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### 1.1 Structural Heterogeneity

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**Example: Conflicts between attributes and attributes**

SSN	FirstName VARCHAR(40)	LastName	Age CHECK(Age > 18)
333-333-3333	Peter	Schmeter	30
333-333-9999	Hans	Glanz	NULL

SSN	FirstName VARCHAR(25)	SurName	Age
3333333333	Peter	Schmeter	30
3333339999	Hans	Glanz	-1

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### 1.1 Structural Heterogeneity

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**Example: Conflicts between attributes and attributes**

SSN	FirstName VARCHAR(40)	LastName	Age CHECK(Age > 18)
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333-333-9999	Hans	Glanz	NULL

SSN	FirstName VARCHAR(25)	SurName	Age
3333333333	Peter	Schmeter	30
3333339999	Hans	Glanz	-1

Conflicting format

Conflicting datatype

synonym

Conflicting constraint

Conflicting default value

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### 1.1 Structural Heterogeneity

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- Normalized vs. denormalized**
  - E.g., relational model: Association between entities can be represented using multiple relations and foreign keys or one relation

**Example**

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### 1.1 Structural Heterogeneity

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- Nested vs. flat**
  - Association between entities can be represented using nesting or references (previous slides)

**Example**

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### 1.1 Structural Heterogeneity

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- Problems caused by schema heterogeneity**
  - Unified access to multiple schemas or integrate schemas into new schema
    - **Schema level:** schema mapping, model management operators, schema languages
    - **Data Level:** virtual data integration, data exchange, warehousing (ETL)

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### 1.1 Heterogeneity +Autonomy

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- Taxonomy of Heterogeneity**

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### 1.1 Semantic Heterogeneity

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- Semantic Heterogeneity**
  - Naming Conflicts
  - Identity Conflicts (Entity resolution)
  - Value Conflicts (Data Fusion)

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### 1.1 Semantic Heterogeneity

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- Naming Conflicts**
  - Ontological (concepts)
    - Birds vs. Animals
  - Synonyms
    - Surname vs. last name
  - Homonyms
  - Units
    - Gallon vs. liter
  - Values
    - Manager vs. Boss


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### 1.1 Semantic Heterogeneity

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- **Ontological concepts**
  - Relationships between concepts
    - $A = B$  - Equivalence
    - $A \subseteq B$  - Inclusion
    - $A \cap B$  - Overlap
    - $A \neq B$  - Disjunction



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### 1.1 Semantic Heterogeneity

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- **Ontological concepts**
  - Relationships between concepts
    - $A = B$  - Equivalence
    - $A \subseteq B$  - Inclusion
    - $A \cap B$  - Overlap
    - $A \neq B$  - Disjunction

**Example**

**Equivalence:** Human vs Homo sapiens  
**Inclusion:** Bird vs Animal  
**Overlap:** Animal vs aquatic lifeform  
**Disjunction:** Fish vs Mammal



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### 1.1 Semantic Heterogeneity

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- **Naming concepts (synonyms)**
  - Different words with same meaning

**Example**

Person (Name, Age)  
 Human (LastName, Age)



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### 1.1 Semantic Heterogeneity

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- **Naming concepts (homonyms)**
  - Same words with different meaning

**Example**

Person (Title, Name)  
 Movie (Title, Year)



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### 1.1 Semantic Heterogeneity

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- **Naming concepts (units)**

**Example**

Person (Title, Name, Salary) \$  
 Person (Title, Name, Salary) CAD




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### 1.1 Semantic Heterogeneity

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- **Identity Conflicts**
  - What is an object?
    - E.g., multiple tuples in relational model
  - Central question:
    - Does object A represent the same entity as B
  - This problem has been called
    - **Entity resolution**
    - **Record linkage**
    - **Deduplication**
    - ...



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## 1.1 Semantic Heterogeneity

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- Identity Conflicts

**Example**

```
(IBM,3000000000,USA)
(International Business Machines Corporation,50000)
```

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## 1.1 Semantic Heterogeneity

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- Value Conflicts
  - Objects representing the same entities have conflicting values for semantically equivalent attributes
    - We have to identified that these objects are represent the same entity first!
  - Resolving such conflicts requires **Data Fusion**
    - Pick value from conflicting values
    - Numerical methods: e.g., average
    - Preferred value
    - ...

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## 1.1 Autonomy

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- How autonomous are data sources
  - One company
    - Can enforce, e.g., schema and software
  - ...
  - The web
    - Website decides
      - Interface
      - Determines access restrictions and limits
      - Availability
      - Format
      - Query restrictions
      - ...

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## 1.2 Data integration tasks

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- Cleaning and preparation
- Entity resolution
- Data Fusion
- Schema matching
- Schema mapping
- Query rewrite
- Data translation

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## 1.3 Data integration architectures

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- Virtual data integration
- Data Exchange
- Peer-to-peer data integration
- Datawarehousing
- Big Data analytics

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## 1.4 Formal Background

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- Query Equivalence
  - Complexity for different query classes
- Query Containment
  - Complexity for different query classes
- Datalog
  - Recursion + Negation
- Integrity Constraints
  - Logical encoding of integrity constraints
- Similarity Measures/Metrics

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### 1.4 Boolean Logic

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- **Boolean Logic (syntax)**
  - **Atomic formulas:**
    - Boolean constants (**true, false**)
    - Boolean Variables (can take Boolean constants as values)
  - **Formulas:**
    - Any atomic formula is also a formula
    - If  $\phi, \psi$  are formulas then the following are also valid formulas:

$\neg \phi$	$\phi \wedge \psi$	
$\phi \vee \psi$	$\phi \rightarrow \psi$	

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### 1.4 Boolean Logic

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- **Boolean Logic (semantics)**
  - **Valuation:**
    - Assign truth values to the variables of a formula
    - Under a valuation a formula evaluates to a Boolean value (true or false)
    - If there exists a valuation that makes the formula  $\psi$  true then the formula  $\psi$  is called **satisfiable**
  - **Semantics:**
    - Expected semantics of Boolean operators:

	$\top \wedge \perp = \perp$
	$\top \wedge \top = \top$
	$\perp \vee \top = \top$
	...

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### 1.4 Boolean Logic

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**Example**

**Formula:**

$$(x \vee y) \wedge \neg z$$

**A possible valuation:**

$$\nu : x = \top, y = \perp, z = \top$$

**Evaluating the formula:**

$$(\top \vee \perp) \wedge \neg \top = \top \wedge \perp = \perp$$

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### 1.4 First-order logic (FO)

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- **Concepts**
  - **Domain of discourse  $\mathbb{D}$** 
    - These are the values that we can bind variables to
    - Values from the domain can also be used as constants in formulas
  - **A set of predicate symbols (each with an arity)**

$$R_1, \dots, R_n$$
    - These represent relations (in the mathematical sense)
  - **An infinite set of variables  $\mathcal{X}$**

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### 1.4 FO Syntax

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- **Terms**
  - **Variables:** any variable from  $\mathcal{X}$  is a term
  - **Constants:** any constant from  $\mathbb{D}$  is a term
- **Atomic formulas:**
  - For any n-ary predicate  $R$  and terms  $t_1, \dots, t_n$   $R(t_1, \dots, t_n)$  is an atomic formula
- **Formulas:**
  - If  $\phi, \psi$  are formulas then the following are also valid formulas:

$\psi \wedge \phi$	$\psi \vee \phi$	$\neg \phi$
$\psi \rightarrow \phi$	$\exists x : \psi$	$\forall x : \psi$

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### 1.4 Free / Bound Variables

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- **Free variables of a formula**
  - All variables not bound by quantifiers

$$free(\neg \psi) = free(\psi)$$

$$free(\psi \wedge \phi) = free(\psi) \cup free(\phi)$$

$$free(\psi \vee \phi) = free(\psi) \cup free(\phi)$$

$$free(\forall x : \psi) = free(\psi) - \{x\}$$

$$free(\exists x : \psi) = free(\psi) - \{x\}$$

$$free(R(t_1, \dots, t_n)) = free(t_1) \cup \dots \cup free(t_n)$$

$$free(x) = \{x\}$$

$$free(c) = \emptyset$$


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### 1.4 FO Semantics

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- **Model  $\mathcal{M}$** 
  - an interpretation of the predicates, i.e., we assign each predicate to a concrete relation
  - We select a domain of discourse  $\mathbb{D}$
- **Valuations  $\mu$  for a formula  $\psi$** 
  - Assigns free variables of  $\psi$  to values from  $\mathbb{D}$
- **Substitutions**
  - Replace all free occurrences of variable  $x$  with  $c$
$$\psi[x \leftarrow c]$$



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### 1.4 FO Semantics

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- **Given a model  $\mathcal{M}$  and valuation  $\mu$** 
  - The “result” of a formula  $\llbracket \psi \rrbracket_{\mathcal{M}, \mu}$ 

$$\llbracket c \rrbracket_{\mathcal{M}, \mu} = c$$

$$\llbracket x \rrbracket_{\mathcal{M}, \mu} = \mu(x)$$

$$\llbracket R(t_1, \dots, t_n) \rrbracket_{\mathcal{M}, \mu} = \begin{cases} \top & \text{if } (\llbracket t_1 \rrbracket_{\mathcal{M}, \mu}, \dots, \llbracket t_n \rrbracket_{\mathcal{M}, \mu}) \in R \\ \perp & \text{otherwise} \end{cases}$$


$$\llbracket \psi \wedge \phi \rrbracket_{\mathcal{M}, \mu} = \llbracket \psi \rrbracket_{\mathcal{M}, \mu} \wedge \llbracket \phi \rrbracket_{\mathcal{M}, \mu}$$

$$\llbracket \psi \vee \phi \rrbracket_{\mathcal{M}, \mu} = \llbracket \psi \rrbracket_{\mathcal{M}, \mu} \vee \llbracket \phi \rrbracket_{\mathcal{M}, \mu}$$

$$\llbracket \neg \psi \rrbracket_{\mathcal{M}, \mu} = \neg \llbracket \psi \rrbracket_{\mathcal{M}, \mu}$$

$$\llbracket \exists x : \psi \rrbracket_{\mathcal{M}, \mu} = \bigvee_{c \in \mathbb{D}} \llbracket \psi[x \leftarrow c] \rrbracket_{\mathcal{M}, \mu}$$

$$\llbracket \forall x : \psi \rrbracket_{\mathcal{M}, \mu} = \bigwedge_{c \in \mathbb{D}} \llbracket \psi[x \leftarrow c] \rrbracket_{\mathcal{M}, \mu}$$



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### 1.4 FO semantics

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**Example**


**Formula:**  $\psi = \forall y : R(x, y)$

**Model:**  $\mathcal{M} = \{R = \{(1, 1), (1, 2), (1, 3)\}\}$

$\mathbb{D} = \{1, 2, 3\}$

**Valuation:**  $\mu(x) = 1$

**Result:**

$$\begin{aligned} & \llbracket \forall y : R(x, y) \rrbracket_{\mathcal{M}, \mu} \\ &= \llbracket R(x, 1) \rrbracket_{\mathcal{M}, \mu} \wedge \llbracket R(x, 2) \rrbracket_{\mathcal{M}, \mu} \wedge \llbracket R(x, 3) \rrbracket_{\mathcal{M}, \mu} \\ &= \llbracket (x, 1) \rrbracket_{\mathcal{M}, \mu} \in R \wedge \llbracket (x, 2) \rrbracket_{\mathcal{M}, \mu} \in R \wedge \llbracket (x, 3) \rrbracket_{\mathcal{M}, \mu} \in R \\ &= (\mu(x), 1) \in R \wedge (\mu(x), 2) \in R \wedge (\mu(x), 3) \in R \\ &= (1, 1) \in R \wedge (1, 2) \in R \wedge (1, 3) \in R \\ &= \top \wedge \top \wedge \top \\ &= \top \end{aligned}$$


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### 1.4 FO Problems

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- **Model checking**
  - Given a model  $\mathcal{M}$  and formula  $\psi$  without free variables
  - Is  $\llbracket \psi \rrbracket_{\mathcal{M}, \mu}$  true?
- **Satisfiability**
  - Given a formula  $\psi$  does there exist a model  $\mathcal{M}$  and valuation  $\mu$  such that  $\llbracket \psi \rrbracket_{\mathcal{M}, \mu}$  is true?



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### 1.4 Integrity constraints

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- **You know some types of integrity constraints already**
  - **Functional dependencies**
    - Keys are a special case
  - **Foreign keys**
    - We have not really formalized that



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### 1.4 Integrity constraints

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- Other types are
  - Conditional functional dependencies
    - **E.g., used in cleaning**
  - Equality-generating dependencies
  - Multi-valued dependencies
  - Tuple-generating dependencies
  - Join dependencies
  - Denial constraints
  - ...



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## 1.4 Integrity constraints

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- How to manage all these different types of constraints?
  - Has been shown that these constraints can be expressed in a logical formalism.
  - Formulas which consist of relational and comparison atoms. Variables represent values
    - $R(x,y,z)$
    - $x = y$



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## 1.4 Integrity Constraints

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**Example**



**Primary Key**  $R(A,B)$  :

$$\forall x, y, z : R(x, y) \wedge R(x, z) \rightarrow y = z$$

**Functional Dependency**  $R(A,B)$  with  $A \rightarrow B$  :

$$\forall x, y, z, a : R(x, y) \wedge R(z, a) \wedge x = z \rightarrow y = a$$

**Foreign Key**  $R(A,B)$ ,  $S(C,D)$  where  $D$  is FK to  $R$  :

$$\forall x, y : S(x, y) \rightarrow \exists z : R(y, z)$$



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## 1.4 Integrity constraints

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- Types of constraints we will use a lot
  - Tuple-generating dependencies (tgds)**
    - Implication with conjunction of relational atoms
    - Foreign keys and schema mappings (later)
$$\forall \vec{x} : \phi(\vec{x}) \rightarrow \exists \vec{y} : \psi(\vec{x}, \vec{y})$$
  - Equality-generating dependencies (egds)**
    - Generalizes keys, FDs
$$\forall \vec{x} : \phi(\vec{x}) \rightarrow \bigwedge_{k=1}^n x_{i_k} = x_{j_k}$$



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## 1.4 Datalog

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- What is Datalog?
  - Prolog for databases (syntax very similar)
  - A logic-based query language
- Queries (Program) expressed as set of rules
 
$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$
- One Q is specified as the answer relation (the relation returned by the query)



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## 1.4 Datalog - Intuition


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- A **Datalog rule**

$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$
- Procedural Interpretation:** For all bindings of variables that makes the RHS true (conjunction) return bindings of  $\vec{x}$

**Example**

```
Q (Name) :- Person (Name, Age) .
Return names of persons
```



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## 1.4 Datalog - Syntax

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- A **Datalog program** is a set of Datalog rules
  - Optionally a distinguished answer predicate
- A **Datalog rule** is
 
$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$
- X's** are lists of variables and constants
- Ri's** are relation names
- Q** is a relation name



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### 1.4 Datalog - Terminology

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- Left-hand side of a rule is called its **head**
- Right-hand side of a rule is called its **body**
- Relation are called **predicates**
- $R(\vec{x})$  is called an **atom**
- An **instance** I of a database is the data
- The **active domain**  $\text{adom}(I)$  of an instance I is the set of all constants that occur in I

$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$

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### 1.4 Datalog - Terminology

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**Example**

$$Q(N) :- \text{Person}(N, A) .$$

N, A are **variables**  
 $Q(N)$ ,  $\text{Person}(N, A)$  are **atoms**  
 $\text{Person}$  and  $Q$  are **predicates**

Name	Age
peter	34
bob	45

**Activate domain**  
 $\text{adom}(I) = \{\text{peter}, \text{bob}, 34, 45\}$

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### 1.4 Datalog - Terminology

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- **Intensional vs. extensional**
  - Extensional database (**edb**)
    - What we usually call database
  - Intensional database (**idb**)
    - Relations that occur in the head of rules (are populated by the query)
- Usually we assume that these do not overlap

$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$

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### 1.4 Datalog - Safety

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- A Datalog program is safe if all its rules are **safe**
- A rule is **safe** if all variables in  $\vec{x}$  occur in at least one  $\vec{x}_i$

$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$

**Example**

$$Q(\text{Name}) :- \text{Person}(\text{Name}, \text{Age}) . \quad \text{(safe)}$$

$$Q(\text{Name}, \text{Sal}) :- \text{Peron}(\text{Name}, \text{Age}) . \quad \text{(unsafe)}$$

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### 1.4 Datalog - Semantics

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- The instance of an idb predicate Q in a datalog program for an edb instance I contains all facts that can be derived by applying rules with Q in the head
- A rule derives a fact  $Q(c)$  if we can find a binding of variables of the rule to constants from  $\text{adom}(I)$  such that  $x$  is bound to  $c$  and the body is true

$$Q(\vec{x}) : -R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$

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### 1.4 Datalog - Semantics

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**Example**

$$Q(N) :- \text{Person}(N, A) .$$

N=peter, A=peter:  $Q(\text{peter}) :- \text{Person}(\text{peter}, \text{peter}) .$   
N=peter, A=bob:  $Q(\text{peter}) :- \text{Person}(\text{peter}, \text{bob}) .$   
**N=peter, A=34:  $Q(\text{peter}) :- \text{Person}(\text{peter}, 34) .$**   
N=bob, A=peter:  $Q(\text{bob}) :- \text{Person}(\text{peter}, \text{peter}) .$   
N=bob, A=bob:  $Q(\text{bob}) :- \text{Person}(\text{peter}, \text{bob}) .$   
**N=bob, A=34:  $Q(\text{bob}) :- \text{Person}(\text{bob}, 34) .$**   
N=34, A=peter:  $Q(34) :- \text{Person}(34, \text{peter}) .$   
N=34, A=bob:  $Q(34) :- \text{Person}(34, \text{bob}) .$   
N=34, A=34:  $Q(34) :- \text{Person}(34, 34) .$

N
peter
bob

**Active domain**  
 $\text{adom}(I) = \{\text{peter}, \text{bob}, 34\}$

Name	Age
peter	34
bob	34

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## 1.4 Datalog

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- Different flavors of datalog
  - Conjunctive query**
    - Only one rule
    - Expressible as Select-project-join (SPJ) query in relational algebra (only equality and AND in selection)
  - Union of conjunctive queries**
    - Also allow union
    - SPJ + set union in relational algebra
    - Rules with the same head in Datalog
  - Conjunctive queries with inequalities**
    - Also allow inequalities, e.g., <

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## 1.4 Datalog

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- Different flavors of datalog
  - Recursion**
    - Rules may have recursion:
      - E.g., head predicate in the body
    - Fixpoint semantics based on immediate consequence operator
  - Negation (first-order queries)**
    - Negated relational atoms allowed
    - Require that every variable used in a negated atom also occurs in at least on positive atom (**safety**)
  - Combined Negation + recursion**
    - Stronger requirements (e.g., stratification)

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## 1.4 Datalog – Semantics (Negation)

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- A rule derives a fact  $Q(c)$  if we can find a binding of variables of the rule to constants from  $\text{adom}(I)$  such that  $x$  is bound to  $c$  and the body is true
- A negated atom  $\text{not } R(X)$  is true if  $R(X)$  is not part of the instance

$$Q(\vec{x}) : \neg R_1(\vec{x}_1), \dots, R_n(\vec{x}_n).$$

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## 1.4 Datalog - Semantics

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**Example**

```
Q(N) :- Person(N,A) , not Lives(N) .
```

N=peter,A=peter: Q(peter) :- Person(peter,peter) ,  
not Lives(peter) .

N=peter,A=bob: Q(peter) :- Person(peter,bob) ,  
not Lives(peter) .

...

N=bob,A=34: Q(bob) :- Person(bob,34) ,  
not Lives(bob) .

...

**Result**

N
bob

**Lives**

Name
peter

**Person**

Name	Age
peter	34
bob	34

**Active domain**

$\text{adom}(I) = \{\text{peter}, \text{bob}, 34\}$

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## 1.4 Datalog

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**Example**

Relation **hop(A,B)** storing edges of a graph.

```
Q2hop(x,z) : hop(x,y) , hop(y,z) .
```

```
Qreach(x,y) : hop(x,y) .
```

```
Qreach(x,z) : Qreach(x,y) , Qreach(y,z) .
```

```
Qnode(x) : hop(x,y) .
```

```
Qnode(x) : hop(y,x) .
```

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## 1.4 Datalog

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**Example**

Relation **hop(A,B)** storing edges of a graph.

```
Qnode(x) : hop(x,y) .
```

```
Qnode(x) : hop(y,x) .
```

```
QnotReach(x,y) : Qnode(x) , Qnode(y) ,
```

```
not Qreach(x,y) .
```

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## 1.4 Datalog versus FO

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- A Datalog rule is a FO implication:  
 $Q(X, Y) : -R(X, Z), R(Z, Y).$

Means

$$\forall x, y : \exists z : R(x, z) \wedge R(z, y) \rightarrow Q(x, y)$$

- Databases can be expressed as rules!  
 $R = \{(Peter, Bob), (Bob, Alice)\}$

$$R(Peter, Bob) : -$$

$$R(Bob, Alice) : -$$

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## 1.4 Model-theoretic semantics

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- The result of a Datalog program P is the smallest model  $\mathcal{M}$  for the program if interpreted as a logical formula
  - Only facts that are justified by the program are included in the query result!

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## 1.4 Free Datalog Systems

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- Datalog Education System (DES)
  - <http://des.sourceforge.net/>
- DLV
  - <http://www.dlvsystem.com/dlv/>

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## 1.4 Containment and Equivalence

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## Definition: Query Equivalence

Query Q is equivalent to Q' iff for every database instance I both queries return the same result

$$Q \equiv Q' \Leftrightarrow \forall I : Q(I) = Q'(I)$$

## Definition: Query Containment

Query Q is contained in query Q' iff for every database instance I the result of Q is contained in the result of Q'

$$Q \sqsubseteq Q' \Leftrightarrow \forall I : Q(I) \subseteq Q'(I)$$

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## 1.4 Equivalence

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- The problem of checking query equivalence is of different complexity depending on the **query language** and whether we consider **set** or **bag semantics**

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## 1.4 Containment and Equiv.

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## Example

$$Q_1(x, y) : R(x, y), R(x, z).$$

$$Q_2(x, y) : R(x, y).$$

$$Q_3(x, x) : R(x, x).$$

$$Q_4(x, y) : R(x, y).$$

$$Q_5(x, x) : R(x, y), R(x, x).$$

$$Q_6(x, z) : R(x, y), R(y, z).$$

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### 1.4 Containment and Equiv.

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**Example**

Relation **hop(A,B)** storing edges of a graph.

$Q_{2hop}(x, z) : hop(x, y), hop(x, z) .$

$Q_{up2Hop}(x, z) : hop(x, y), hop(x, z) .$   
 $Q_{up2Hop}(x, z) : hop(x, z) .$

$Q_{sym}(x, y) : hop(x, y) .$   
 $Q_{sym}(x, y) : hop(y, x) .$

$Q_{sym2Hop}(x, y) : Q_{sym}(x, y), Q_{sym}(y, z) .$

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### 1.4 Complexity of Eq. and Cont.

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Set semantics	Relational Algebra	Conjunctive Queries (CQ)	Union of Conjunctive Queries (UCQ)	Monotone Queries/CQ $\neq$
Query Evaluation (Combined Complexity)	PSPACE-complete	NP-complete	NP-complete	NP-complete
Query Evaluation (Data Complexity)	LOGSPACE (that means in P)	LOGSPACE (that means in P)	LOGSPACE (that means in P)	LOGSPACE (that means in P)
Query Equivalence	Undecidable	NP-complete	NP-complete	$\Pi^2$ -complete
Query Containment	Undecidable	NP-complete	NP-complete	$\Pi^2$ -complete

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### 1.4 Complexity of Eq. and Cont.

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Bag semantics	Relational Algebra	Conjunctive Queries (CQ)	Union of Conjunctive Queries (UCQ)
Query Equivalence	Undecidable	Equivalent to graph isomorphism	Undecidable
Query Containment	Undecidable	<b>Open Problem</b>	Undecidable

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### 1.4 Containment Mappings

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- NP-completeness for set semantics CQ and UCQ for the containment, evaluation, and equivalence problems is based on reducing these problems to the same problem
  - [Chandra & Merlin, 1977]
- Notational Conventions:
  - **head(Q)** = variables in head of query Q
  - **body(Q)** = atoms in body of Q
  - **vars(Q)** = all variable in Q

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### 1.4 Boolean Conjunctive Queries

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- A conjunctive query is boolean if the head does not have any variables
  - **Q() :- hop(x,y), hop(y,z)**
  - We will use  $Q :- \dots$  as a convention for  $Q() :- \dots$
  - What is the result of a Boolean query
    - Empty result {}, e.g., no **hop(x,y), hop(y,z)**
    - If there are tuples matching the body, then a tuple with zero attributes is returned {}
  - > We interpret {} as **false** and {} as **true**
  - Boolean query is essentially an existential check

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### 1.4 Boolean Conjunctive Queries

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**Example**

Hop relation: Hop(A,B)

$Q :- hop(x, y)$

SELECT EXISTS (SELECT \* FROM hop)

Note: in Oracle and DB2 we need a from clause

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## 1.4 Boolean Conjunctive Queries

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**Example**

```
SELECT
  CASE WHEN EXISTS (SELECT *
                    FROM hop)
  THEN 1 ELSE 0
  END AS x
FROM dual;
```

Notes:

- Oracle and DB2 FROM not optional
- Oracle has no boolean datatype

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## 1.4 Boolean Conjunctive Queries

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- BCQ in SQL

**Example**

```
Q :- hop(x,y), hop(y,z)

SELECT EXISTS
  (SELECT *
   FROM hop l, hop r
   WHERE l.B = r.A)
```

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## 1.4 Containment Mappings

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- How to check for containment of CQs (set)

**Definition: Variable Mapping**

A variable mapping  $\psi$  from query  $Q$  to query  $Q'$  maps the variables of  $Q$  to constants or variables from  $Q'$

**Definition: Containment Mapping**

A containment mapping from query  $Q$  to  $Q'$  is a variable mapping  $\psi$  such that:

$$\Psi(head(Q)) = head(Q')$$

$$\forall R(\vec{x}_i) \in body(Q) : \Psi(R(\vec{x}_i)) \in body(Q')$$

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## 1.4 Containment Mappings

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**Theorem: Containment Mappings and Query Containment**

Query  $Q$  is contained in query  $Q'$  iff there exists a containment mapping  $\psi$  from  $Q'$  to  $Q$

$$Q \sqsubseteq Q' \Leftrightarrow \exists \Psi : \Psi \text{ is a containment mapping } Q' \rightarrow Q$$

**Example**

```
Q1(u,z) : R(u,z) .
Q2(x,y) : R(x,y) .
```

Can we find a containment mapping?

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## 1.4 Containment Mappings

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**Theorem: Containment Mapping and Query Containment**

Query  $Q$  is contained in query  $Q'$  iff there exists a containment mapping  $\psi$  from  $Q'$  to  $Q$

**Example**

```
Q1(u,z) : R(u,z) .
Q2(x,y) : R(x,y) .
```

$Q_1 \rightarrow Q_2 : \Psi(u) = x, \Psi(z) = y$

$Q_2 \rightarrow Q_1 : \Psi(x) = u, \Psi(y) = z$

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## 1.4 Containment Mappings

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**Example**

```
Q1(a,b) : R(a,b), R(b,c) .
Q2(x,y) : R(x,y) .
```

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### 1.4 Containment Mappings

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**Example**

$$Q_1(a, b) : R(a, b), R(b, c).$$

$$Q_2(x, y) : R(x, y).$$

Do containment mappings exist?

$Q_1 \rightarrow Q_2$ : none exists  
 $Q_2 \rightarrow Q_1$ :  $\Psi(x) = a, \Psi(y) = b$

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### 1.4 Containment Mappings

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**Example**

$$Q_1(a, b) : R(a, b), R(c, b).$$

$$Q_2(x, y) : R(x, y).$$

$Q_1 \rightarrow Q_2$ :  $\Psi(a) = x, \Psi(b) = y, \Psi(c) = x$   
 $Q_2 \rightarrow Q_1$ :  $\Psi(x) = a, \Psi(y) = b$

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### 1.4 Containment Background

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- It was shown that query evaluation, containment, equivalence as all reducible to homomorphism checking for CQ
  - Canonical conjunctive query  $Q^I$  for instance  $I$ 
    - Interpret attribute values as variables
    - The query is a conjunction of all atoms for the tuples
    - $I = \{\text{hop}(a,b), \text{hop}(b,c)\} \rightarrow Q^I :- \text{hop}(a,b), \text{hop}(b,c)$
  - Canonical instance  $I^Q$  for query  $Q$ 
    - Interpret each conjunct as a tuple
    - Interpret variables as constants
    - $Q :- \text{hop}(a,a) \rightarrow I^Q = \{\text{hop}(a,a)\}$

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### 1.4 Containment Background

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- Containment Mapping  $\leftrightarrow$  Containment
- Proof idea (boolean queries)
  - (if direction)
    - Assume we have a containment mapping  $Q_1$  to  $Q_2$
    - Consider database  $D$
    - $Q_2(D)$  is true then we can find a mapping from  $\text{vars}(Q_2)$  to  $D$
    - Compose this with the containment mapping and prove that this is a result for  $Q_1$

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### 1.4 Containment Mappings

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**Example**

$$Q_1() : R(a, b), R(c, b).$$

$$Q_2() : R(x, y).$$

$$Q_2 \rightarrow Q_1 : \Psi(x) = a, \Psi(y) = b$$

$D = \{R(1, 1), R(1, 2)\}$

$Q_1(D) = \{(1, 1), (1, 2)\}$   
 $\phi(a) = 1, \phi(b) = 2, \phi(c) = 1$

$\Psi_\phi(x) = 1, \Psi_\phi(y) = 2$

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### 1.4 Containment Background

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- Containment Mapping  $\leftrightarrow$  Containment
- Proof idea (boolean queries)
  - (only-if direction)
    - Assume  $Q_2$  contained in  $Q_1$
    - Consider canonical (frozen) database  $I^{Q_2}$
    - Evaluating  $Q_1$  over  $I^{Q_2}$  and taking a variable mapping that is produced as a side-effect gives us a containment mapping

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### 1.4 Containment Mappings

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**Example**

$$Q_1() : R(a, b), R(c, b).$$

$$Q_2() : R(x, y).$$

$$Q_2 \rightarrow Q_1 : \Psi(x) = a, \Psi(y) = b$$

$$I^{Q_1} = \{(a, b), (c, b)\}$$

$$Q_2(I^{Q_1}) = \{()\}$$

$$\varphi(x) = a, \varphi(y) = b$$

$\varphi$  is our containment mapping  $\Psi$

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### 1.4 Containment Background

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- If you are not scared and want to know more:
  - Look up Chandra and Merlins paper(s)
  - The text book provides a more detailed overview of the proof approach
  - Look at the slides from Phokion Kolaitis excellent lecture on database theory
    - <https://classes.soe.ucsc.edu/cms277/Winter10/>

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### 1.4 Containment Background

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- A more intuitive explanation why containment mappings work
  - Variable naming is irrelevant for query results
  - If there is a containment mapping  $Q$  to  $Q'$ 
    - Then every condition enforced in  $Q$  is also enforced by  $Q'$
    - $Q'$  may enforce additional conditions

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### 1.4 Containment Mappings

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**Example**

$$Q_1() : R(a, b), R(c, b).$$

$$Q_2() : R(x, y).$$

$$Q_2 \rightarrow Q_1 : \Psi(x) = a, \Psi(y) = b$$

If there exists tuples  $R(a, b)$  and  $R(c, b)$  in  $R$  that make  $Q_1$  true, then we take  $R(a, b)$  to fulfill  $Q_2$

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### 1.4 Containment Background

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- From boolean to general conjunctive queries
  - Instead of returning true or false, return bindings of variables
  - Recall that containment mappings enforce that the head is mapped to the head
  - $\rightarrow$  same tuples returned, but again  $Q'$ 's condition is more restrictive

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### 1.4 Containment Mappings

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**Example**

$$Q_1(a) : R(a, b), R(c, b).$$

$$Q_2(x) : R(x, y).$$

$$Q_2 \rightarrow Q_1 : \Psi(x) = a, \Psi(y) = b$$


For every  $R(a, b)$  and  $R(c, b)$   $Q_1$  returns  $(a)$  and for every  $R(a, b)$   $Q_2$  returns  $(a)$

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1.4 Similarity Measures ILLINOIS INSTITUTE OF TECHNOLOGY

- **Problem faced by multiple integration tasks**
  - Given two objects, how similar are they
  - **E.g., given two attribute names in schema matching, given two values in data fusion/entity resolution, ...**




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1.4 Similarity Measures ILLINOIS INSTITUTE OF TECHNOLOGY

- **Object models**
  - **Multidimensional (feature vector model)**
    - Object is described as a vector of values - one for each dimension out of a given set of dimensions
    - E.g., Dimensions are gender (male/female), age (0-120), and salary (0-1,000,000). An example object is [male,80,70,000]
  - **Strings**
    - E.g., how similar is “Poeter” to “Peter”
  - **Graphs and Trees**
    - E.g., how similar are two XML models



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1.4 Similarity Measures ILLINOIS INSTITUTE OF TECHNOLOGY

**Definition: Similarity Measure**

Function  $d(p,q)$  where  $p$  and  $q$  are objects, that returns a real score with

- $d(p,p) = 0$
- $d(p,q) \geq 0$

- **Interpretation: the lower the score the “more similar” the objects are**
- We require  $d(p,p)=0$ , because nothing can be more similar to an object than itself
- **Note: often scores are normalized to the range [0,1]**



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1.4 Similarity Measures ILLINOIS INSTITUTE OF TECHNOLOGY

**Example**

**String equality:**  $d(p,q) = 0$  if  $p=q$   
 $d(p,q) = 1$  else

**Euclidian distance:**  $d(p,q) = \sqrt{\sum_{i=1}^n (p[i] - q[i])^2}$   
 N-dimensional space

**Edit distance:**  $d(p,q) =$  minimum number of single character insertions, deletions, replacements to transform  $p$  into  $q$

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1.4 Similarity Measures ILLINOIS INSTITUTE OF TECHNOLOGY

**Definition: Metric**

Function  $d(p,q)$  where  $p$  and  $q$  are objects, that returns a real score with

- **Non-negative**  $d(p,q) \geq 0$
- **Symmetry**  $d(p,q) = d(q,p)$
- **Identity of indiscernibles**  $d(p,q) = 0$  iff  $p=q$
- **Triangle inequality**  $d(p,q) + d(q,r) \geq d(p,r)$



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1.4 Similarity Measures ILLINOIS INSTITUTE OF TECHNOLOGY

**Definition: Metric**

Function  $d(p,q)$  where  $p$  and  $q$  are objects, that returns a real score with

- **Non-negative**  $d(p,q) \geq 0$
- **Symmetry**  $d(p,q) = d(q,p)$
- **Identity of indiscernibles**  $d(p,q) = 0$  iff  $p=q$
- **Triangle inequality**  $d(p,q) + d(q,r) \geq d(p,r)$




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## 1.4 Similarity Measures

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- **Why do we care whether  $d$  is a metric?**
  - Some data mining algorithms only work for metrics
    - E.g., some clustering algorithms such as k-means
    - E.g., clustering has been used in entity resolution
  - Metric spaces allow optimizations of some methods
    - E.g., Nearest Neighborhood-search: find the most similar object to an object  $p$ . This problem can be efficiently solved using index structures that only apply to metric spaces


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## Summary

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- Heterogeneity
  - Types of heterogeneity
  - Why do they arise?
  - Hint at how to address them
- Autonomy
- Data Integration Tasks
- Data Integration Architectures
- Background
  - Datalog + Query equivalence/containment + Similarity + Integrity constraints


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## Outline

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- 0) Course Info
- 1) Introduction
- 2) Data Preparation and Cleaning**
- 3) Schema matching and mapping
- 4) Virtual Data Integration
- 5) Data Exchange
- 6) Data Warehousing
- 7) Big Data Analytics
- 8) Data Provenance

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